

# Long Division of Polynomials

What method can I use to divide polynomials?

- let's use area models (inverse of multiplying binomials)
- start from inside out
- first term of polynomial
- divisor goes outside model
- should lose a "variable" each time

Let's practice!

Example #1:  $6x^3 - 19x^2 + 16x - 4 \div x - 2$

$$\begin{array}{r} 6x^2 - 7x + 2 \\ \hline x \left| \begin{array}{cccc} 6x^3 & -7x^2 & 2x & 0 \\ -2 \left| \begin{array}{cccc} -12x^2 & +14x & -4 & \end{array} \right. \end{array} \right. \end{array} = 6x^2 - 7x + 2 \quad \text{(no R)}$$

$$-12x^2 - 7x^2 = 19x^2$$

$$14x + 2x = 16x$$

$$-4 + 0 = -4$$

Example #2:  $x^3 - 3x^2 + 8 \checkmark x - 5 \div x - 1$

$$\begin{array}{c} x^2 - 2x + b \\ \hline x | x^3 & -2x^2 & +6x + 1 \\ -1 | -x^2 & +2x & -6 \end{array}$$

$= (x^2 - 2x + b) + \frac{1}{x-1}$

$$\begin{aligned} -x^2 - 2x^2 &= -3x^2 \\ +2x + 6x &= 8x \\ -6 + 1 &= -5 \end{aligned}$$

can't divide by  $x$  because that's the last term  
 $= 1$  is the remainder

Example #3:  $2x^4 - x^3 + 4 \checkmark \div x + 1$

$$\begin{array}{c} 2x^3 - 3x^2 + 3x - 3 \\ \hline x | 2x^4 & -3x^3 & 3x^2 & -3x & \text{remainder} \\ +1 | +2x^3 & -3x^2 & +3x & -3 \end{array}$$

$= (2x^3 - 3x^2 + 3x - 3) + \frac{7}{x+1}$

$$\begin{aligned} 2x^3 - 3x^3 &= -x^3 \\ -3x^2 + 3x^2 &= 0 \\ 3x - 3x &= 0 \quad \text{no term} \\ -3 + 7 &= 4 \end{aligned}$$